# 3950202 061

# REPORT DOCUMENTATION PAGE

Form Approved OMB No. 0704-0188

Public reporting burden for this follection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Services, Directorate for information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302, and to the Office of Management and Budget, Paperwork Reduction Project (0704-0188), Washington, DC 20503

FEB 0 6 1995

1. AGENCY USE ONLY (Leave blank)

2. REPORT DATE November 15, 1994 3. REPORT TYPE AND DATES COVERED Final Report, 4/10/91 - 9/30/94

5. FUNDING NUMBERS

4. TITLE AND SUBTITLE

Analytical theory of continued fractions and time evolution in many-particle systems.

6. AUTHOR(S)

M. Howard Lee

DAAG03-91-6-0108

7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES)

Department of Physics and Astronomy The University of Georgia Athens, Georgia 30602-2451

8. PERFORMING ORGANIZATION REPORT NUMBER

9. SPONSORING/MONITORING AGENCY NAME(S) AND ADD

U.S. Army Research Office P. O. Box 12211 Research Triangle Park, NC 27709-2211 10. SPONSORING / MONITORING AGENCY REPORT NUMBER

ARO 27580.7 -MA

11. SUPPLEMENTARY NOTES

The view, opinions and/or findings contained in this report are those of the author(s) and should not be construed as an official Department of the Army position, policy, or decision, unless so designated by other documentation.

12a. DISTRIBUTION / AVAILABILITY STATEMENT

12b. DISTRIBUTION CODE

Approved for public release; distribution unlimited.

13. ABSTRACT (Maximum 200 words)

The analytical theory of continued fractions plays a key role in the time evolution behavior in many-particle systems. The aim of this study was to understand and to develop properties of relevant continued fractions for physical applications. Substantial progress has been made and reported in eleven (11) journal articles and several other conference proceedings also published.

14. SUBJECT TERMS

Grant

DEIG COMMUNICATION A

15. NUMBER OF PAGES 3/including this pg 16. PRICE CODE

SECURITY CLASSIFICATION OF REPORT UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE UNCLASSIFIED

SECURITY CLASSIFICATION OF ABSTRACT UNCLASSIFIED

20. LIMITATION OF ABSTRACT UL

## GENERAL INSTRUCTIONS FOR COMPLETING SF 298

The Report Documentation Page (RDP) is used in announcing and cataloging reports. It is important that this information be consistent with the rest of the report, particularly the cover and title page. Instructions for filling in each block of the form follow. It is important to stay within the lines to meet optical scanning requirements.

- Block 1 Agency Use Only (Leave blank)
- Block 2. Report Date Full publication date including day, month, and year, if available (e.g. 1 Jan 88). Must cite at least the year.
- Block 3. Type of Report and Dates Covered. State whether report is interim, final, etc. If applicable, enter inclusive report dates (e.g. 10 Jun 87 30 Jun 88).
- Block 4. <u>Title and Subtitle</u>. A title is taken from the part of the report that provides the most meaningful and complete information. When a report is prepared in more than one volume, repeat the primary title, add volume number, and include subtitle for the specific volume. On classified documents enter the title classification in parentheses.
- **Block 5.** <u>Funding Numbers</u>. To include contract and grant numbers; may include program element number(s), project number(s), task number(s), and work unit number(s). Use the following labels:

C - Contract PR - Project
G - Grant TA - Task
PF - Program WII - Work I

PE - Program WU - Work Unit Element Accession No.

- Block 6. <u>Author(s)</u>. Name(s) of person(s) responsible for writing the report, performing the research, or credited with the content of the report. If editor or compiler, this should follow the name(s).
- **Block 7.** <u>Performing Organization Name(s) and Address(es)</u>. Self-explanatory.
- Block 8. <u>Performing Organization Report</u>
  <u>Number.</u> Enter the unique alphanumeric report number(s) assigned by the organization performing the report.
- Block 9. Sponsoring/Monitoring Agency Name(s) and Address(es). Self-explanatory.
- Block 10. <u>Sponsoring/Monitoring Agency</u> Report Number. (If known)
- Block 11. <u>Supplementary Notes</u>. Enter information not included elsewhere such as: Prepared in cooperation with...; Trans. of...; To be published in.... When a report is revised, include a statement whether the new report supersedes or supplements the older report.

Block 12a. <u>Distribution/Availability Statement</u>. Denotes public availability or limitations. Cite any availability to the public. Enter additional limitations or special markings in all capitals (e.g. NOFORN, REL, ITAR).

DOD - See DoDD 5230.24, "Distribution Statements on Technical Documents."

DOE - See authorities.

NASA - See Handbook NHB 2200.2.

NTIS - Leave blank.

Block 12b. Distribution Code.

DOD - Leave blank.

DOE - Enter DOE distribution categories from the Standard Distribution for Unclassified Scientific and Technical Reports.

NASA - Leave blank. NTIS - Leave blank.

- Block 13. Abstract. Include a brief (Maximum 200 words) factual summary of the most significant information contained in the report.
- Block 14. <u>Subject Terms</u>. Keywords or phrases identifying major subjects in the report.
- **Block 15.** <u>Number of Pages</u>. Enter the total number of pages.
- **Block 16.** <u>Price Code</u>. Enter appropriate price code (NTIS only).
- Blocks 17. 19. Security Classifications. Self-explanatory. Enter U.S. Security Classification in accordance with U.S. Security Regulations (i.e., UNCLASSIFIED). If form contains classified information, stamp classification on the top and bottom of the page.
- Block 20. <u>Limitation of Abstract</u>. This block must be completed to assign a limitation to the abstract. Enter either UL (unlimited) or SAR (same as report). An entry in this block is necessary if the abstract is to be limited. If blank, the abstract is assumed to be unlimited.

# FINAL REPORT

ARO Grant #27580MA

Title: "Analytical Theory of Continued Fractions and Time Evolution in Many-Body Systems." Principal Investigator: M. Howard Lee, Department of Physics and Astronomy, The University of Georgia, Athens. Georgia 30602-2451

### Problems Studied -A.

The analytical theory of continued fractions plays a key role in out understanding of time evolution in many-particle systems. The continued fractions that appear in these physical problems are highly specialized. The aim of this study was to understand and to develop the properties of relevant continued fractions for physical applications.

### Most Important Results -В.

The two most important results of our study are given in our publications #3 and #7 (see C below). The paper #3 shows that important scattering results can be obtained by the time evolution approach developed by us. The paper #7 shows that exact results for scattering cross sections can be obtained by the method of continued fractions developed by us.

### C. Publication Lists -

- M. Long and M. H. Lee 1. The classical susceptibility of a free electron gas. J. Math. Phys. 33, 1799 (1992)
- 2. M. H. Lee Slow Decay in a spin system and spin precession. Kor. J. Phys. 24, 558 (1992)
- M. H. Lee and O. I. Sindoni 3. Dynamic response function and Kramers-Kronig relations in optic inversion. Phys. Rev. A 46, 3028 (1992)
- 4. M. H. Lee Summary talk with a few reflections. Kor. J. Phys. 24, S111 (1992)
- 5. M. H. Lee Velocity autocorrelation function in hydrodynamics. J. Phys. Condensed Matter 4, 10487 (1992)

Accesion For		
NTIS		X
DTIC		
Unannounced		
Justification		
By		
Availability Codes		
Dist	Avail and or Special	
A-1		

# C. Publication Lists - (continued)

6. M. H. Lee
Autocorrelation functions for Hermitian many-body systems.
Phys. Rev. B 47, 8293 (1993)

7. J. Hong and M. H. Lee
Asymptotically exact solution of the dynamic structure factor.
Phys. Rev. Lett. 70, 1972 (1993)

8. M. H. Lee
Note on a log integral for the plasma energy.
Can. J. Phys. 1994 (accepted)

9. M. H. LeePolylogarithmic analysis of the chemical potential.J. Math. Phys. 1994 (accepted)

10. M. H. LeePrice's bound on the structure factor.J. Math. Phys. 1994 (accepted)

 M. H. Lee, J. Kim, W. P. Cummings and R. Dekeyser Topology of Hilbert spaces and dynamics of molecular processes.
 J. Mol. Str. 1994 (accepted)

# D. List of Participants -

M. H. Lee - Principal Investigator
M. Long - Graduate Student, received Ph.D. in 1994